## Review for Unit 4 Test

1 For  $0 \le t \le 13$ , an object travels along an elliptical path given parametrically by  $\begin{cases} x = 3\cos t \\ y = 4\sin t \end{cases}$ . At the point at which

t=13, the object leaves the path and travels along the line tangent to the path at that point. What is the slope of the line on which the object travels?

$$a - \frac{4}{3}$$

$$b - \frac{3}{4}$$

$$c = -\frac{4\tan 1}{3}$$

a 
$$-\frac{4}{3}$$
 b  $-\frac{3}{4}$  c  $-\frac{4 \tan 13}{3}$  d  $-\frac{4}{3 \tan 13}$  e  $-\frac{3}{4 \tan 13}$ 

$$e = \frac{3}{4\tan 13}$$

2 The position of a particle moving in the xy-plane is given by the parametric equations  $\begin{cases} x = t^3 - 3t^2 \\ y = 2t^3 - 3t^2 - 12t \end{cases}$ . For what

values of t is the particle at rest?

$$\binom{c}{c}$$
 2 only

b 0 only 
$$\binom{c}{2}$$
 only  $\binom{d}{d} - 1$  and 2 only  $\binom{e}{d} - 1$ , 0, and 2

3 A curve C is defined by the parametric equations  $\begin{cases} x = t^2 - 4t + 1 \\ y = t^3 \end{cases}$ . Which of the following is an equation of the line

tangent to the graph of C at the point (-3,8)?

**b** 
$$x = 2$$

$$c y = 8$$

b 
$$x=2$$
 c  $y=8$  d  $y=-\frac{27}{10}(x+3)+8$  e  $y=12(x+3)+8$ 

4 A particle moves so that its position at time t is given by  $\begin{cases} x = t^2 \\ y = \sin(4t) \end{cases}$ . What is the speed of the particle when t = 3?  $a - 8\sin 12 \qquad b \frac{4\cos 12}{6} \qquad (c) \sqrt{(4\cos 12)^2 + 36} \qquad d \sqrt{(\sin 12)^2 + 81} \qquad e (4\cos 12)^2 + 36$ 

$$b \frac{4\cos 12}{6}$$

$$\left(c\right)\sqrt{\left(4\cos 12\right)^2+36}$$

$$d \sqrt{\left(\sin 12\right)^2 + 81}$$

$$e (4\cos 12)^2 + 36$$

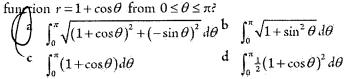
5 Which of the following integrals represents the area shaded in the graph shown at right? The curve is given by  $r = 4 \sin 2\theta$ .

a 
$$\int_{3\pi/2}^{2\pi} 2\sin(2\theta)d\theta$$
 b  $\int_{\pi/2}^{\pi} 8\sin^2(2\theta)d\theta$  c  $\int_0^{\pi} 2\sin^2(2\theta)d\theta$ 

$$c \int_0^{\pi} 2\sin^2(2\theta)d\theta$$

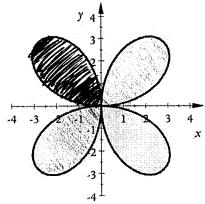
$$d \int_{\pi/2}^{\pi} 2\sin(2\theta) d\theta e \int_{3\pi/2}^{2\pi} 4\sin^2(2\theta) d\theta$$

6 Which of the following integrals represents the arc length of the polar



$$\int_0^{\pi} \sqrt{1 + \sin^2 \theta} d\theta$$

$$e \int_0^{\pi} 2\pi (1+\cos\theta)\sin\theta \sqrt{(1+\cos\theta)^2+(-\sin\theta)^2} d\theta$$



7 Consider the graph of the vector function  $\mathbf{r}(t) = \langle 1 + t^3, 3 + 4t \rangle$ . What is the value of  $\frac{d^2y}{dx^2}$  at the point on the graph where x = 2?

- b  $\frac{4}{3}$   $c \frac{8}{3}$   $\binom{d}{-\frac{8}{9}}$   $e \frac{1}{18}$

8 A particle proves so that at time t > 0 its position vector is  $\langle \ln(t^2 + 2t), 2t^2 \rangle$ . At time t = 2, its velocity vector is

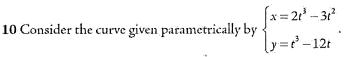


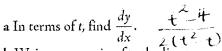
- b  $\langle \frac{3}{4}, 4 \rangle$  c  $\langle \frac{1}{8}, 8 \rangle$  d  $\langle \frac{1}{8}, 4 \rangle$  e  $\langle -\frac{5}{16}, 4 \rangle$

х

9 Consider the curves  $r_1 = 2\cos\theta$  and  $r_2 = \sqrt{3}$ .

- a Sketch the curves on the axes provided at right.
- b Show use of calculus to find the area of the region common to 2.799 both graphs.

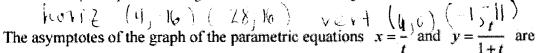




- a In terms of t, find  $\frac{dx}{dx}$ .

  b Write an equation for the line tangent to the curve at the point at which t=-1.

  c Find the x- and y-coordinates for each critical point on the curve
- and identify each point as having a vertical or horizontal tangent.



(Hint: rewrite the curve in rectangular coordinates, then find its asymptotes.)

(A) 
$$x = 0, y = 0$$

11.

(B) 
$$x = 0$$
 only

(D) 
$$x = -1$$
 only

(E) 
$$x = 0, y = 1$$

(C) 
$$x = -1, y = 0$$

## CALCULATOR-ACTIVE

12 An object moving along a curve in the xy-plane has position (x(t), y(t)) at time  $t \ge 0$  with  $\frac{dx}{dt} = 12t - 3t^2$  and

 $\frac{dy}{dt} = \ln(1+(t-4)^4)$ . At time t=0, the object is at position (-13,5). At time t=2, the object is at point P with xcoordinate 3.

- a Find the acceleration vector and the speed at time t=2,  $\langle e \rangle = 1.8827 + 12.337$
- b Find the y-coordinate of point  $P_1 = 13$ . (c. 7) c Write an equation for the line tangent to the curve at point  $P_2 = 43$ . (c. 7) = 236. (x-3)
- d For what value(s) of t, if any, is the object at rest? Justify your answer.

