

Use the definition of a derivative to find the derivative of each function with respect to x.

1. $f(x) = -2x + 5$ -2

2. $f(x) = 4x^2 + 1$ $8x$

3. $f(x) = 3x^2 + 3x + 3$ $(6x + 3)$

4. $f(x) = \sqrt{4x - 5}$ $\frac{2}{\sqrt{4x-5}}$

5. $f(x) = \frac{1}{x+2}$ $-\frac{1}{(x+2)^2}$

$$5. f'(x) = \lim_{h \rightarrow 0} \frac{\frac{1}{x+h+2} - \frac{1}{x+2}}{h}$$

$$= \lim_{h \rightarrow 0} \frac{x+2 - (x+h+2)}{(x+h+2)(x+2) \cdot h}$$

$$= \lim_{h \rightarrow 0} \frac{x+2 - x - h - 2}{(x+h+2)(x+2) \cdot h} \cdot \frac{1}{h}$$

$$= \lim_{h \rightarrow 0} \frac{-h}{(x+h+2)(x+2) \cdot h} = \frac{-1}{(x+2)^2}$$

3. $f'(x) = \lim_{h \rightarrow 0} \frac{3(x+h)^2 + 3(x+h) + 3 - (3x^2 + 3x + 3)}{h}$

$$= \lim_{h \rightarrow 0} \frac{3x^2 + 6hx + 3h^2 + 3x + 3h + 3 - 3x^2 - 3x - 3}{h}$$

$$= \lim_{h \rightarrow 0} \frac{(6x + 3)h + 3h^2}{h} = 6x + 3$$

4. $f'(x) = \lim_{h \rightarrow 0} \frac{\sqrt{4(x+h) - 5} - \sqrt{4x - 5}}{h} \cdot \left(\frac{\sqrt{4(x+h) - 5} + \sqrt{4x - 5}}{\sqrt{4(x+h) - 5} + \sqrt{4x - 5}} \right)$

$$= \lim_{h \rightarrow 0} \frac{4(x+h) - 5 - (4x - 5)}{h(\sqrt{4(x+h) - 5} + \sqrt{4x - 5})} = \lim_{h \rightarrow 0} \frac{4x + 4h - 5 - 4x + 5}{h(\sqrt{4(x+h) - 5} + \sqrt{4x - 5})}$$

$$= \lim_{h \rightarrow 0} \frac{4h}{h(\sqrt{4(x+h) - 5} + \sqrt{4x - 5})} = \frac{4}{\sqrt{4x-5} + \sqrt{4x-5}} = \frac{4}{2\sqrt{4x-5}}$$