

### Practice Section 5.1: Simplifying Trigonometric Expressions

Use basic trigonometric identities to simplify. Show all substitutions and algebra.

1.  $(\tan \theta)(\cos \theta)$

$$\sin \theta$$

2.  $\csc x - \cos x \cot x$

$$\sin x$$

3.  $(\tan \theta)(\cot \theta)$

$$1$$

4.  $\sin x + \sin x \cot^2 x$

$$\csc x$$

5.  $\cos^2 \theta + \sin^2 \theta$

$$1$$

6.  $(\sin \theta - 1)(\sin \theta + 1)$

$$-\cos^2 \theta$$

7.  $(\csc \theta - 1)(\csc \theta + 1)$

$$\cot^2 \theta$$

8.  $\cos \theta (\sec \theta - \cos \theta)$

$$\sin^2 \theta$$

9.  $(\cot \theta)(\sec \theta)(\sin \theta)$

$$1$$

10.  $(\sec \theta - \tan \theta)(\sec \theta + \tan \theta)$

$$1$$

11.  $\frac{\sin \theta \cos \theta}{1 - \cos^2 \theta}$

$$\cot \theta$$

12.  $\frac{1}{\sec^2 \theta} + \frac{1}{\csc^2 \theta}$

$$1$$

13.  $\frac{\tan \theta \cos \theta}{\sin \theta}$

$$1$$

14.  $\cos^2 \theta + (\tan^2 \theta)(\cos^2 \theta)$

$$1$$

15.  $1 + (\csc^2 \theta)(\cos^2 \theta)$

$$\csc^2 \theta$$

16.  $\sin \theta \csc(-\theta)$

$$-1$$

17.  $\sec \theta \sin\left(\frac{\pi}{2} - \theta\right)$

$$1$$

18.  $\sec^2(-\theta) - \tan^2 \theta$

$$1$$

|  |
|--|
| <b>Simplifying Trigonometric Expressions</b> |
|--|

Simplify each of the following.

1.  $\sec x \cos x$

$1$

3.  $\tan^2 x - \sec^2 x$

$-1$

5.  $\cot x \sin x$

$\cos x$

7.  $\sin x \sec x$

$\tan x$

9.  $\frac{\sec^2 x - 1}{\sin^2 x}$

$\sec^2 x$

11.  $\sec^4 x - \tan^4 x$

$\sec^2 x + \tan^2 x$

13.  $\tan \theta \csc \theta$

$\sec \theta$

15.  $\cos \beta \tan \beta$

$\sin \beta$

17.  $\frac{\cot x}{\csc x}$

19.  $\sec^2 x (1 - \sin^2 x)$

2.  $\frac{\sin(-x)}{\cos(-x)}$

4.  $\frac{1 - \cos^2 x}{\sin x}$

6.  $\frac{\sin\left(\frac{\pi}{2} - x\right)}{\cos\left(\frac{\pi}{2} - x\right)}$

8.  $\cos^2 x (\sec^2 x - 1)$

10.  $\cot x \sec x$

12.  $\frac{\cos^2\left(\frac{\pi}{2} - x\right)}{\cos x}$

14.  $\sin \theta (\csc \theta - \sin \theta)$

16.  $\sec \alpha \frac{\sin \alpha}{\tan \alpha}$

18.  $\frac{\csc \theta}{\sec \theta}$

20.  $\frac{1}{\tan^2 x + 1}$