

Find all solutions for each equation:

1. $2\cos x - 1 = 0 \quad \frac{\pi}{3} + 2\pi k, \frac{5\pi}{3} + 2\pi k$

2. $4\csc \theta + 6 = -2 \quad \frac{\pi}{6} + 2\pi k, \frac{11\pi}{6} + 2\pi k$

Find all values of x on the interval $[0, 2\pi)$.

3. $2\sin^2 x - 1 = 0 \quad \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$

4. $2\cos^2 x + \cos x = 0 \quad \frac{\pi}{2}, \frac{3\pi}{2}, \frac{2\pi}{3}, \frac{4\pi}{3}$

5. $\sqrt{3}\cot x + 1 = 0 \quad \frac{2\pi}{3}, \frac{5\pi}{3}$

6. $1 - \cos^2 x = 1 + \cos x + \cos^2 x \quad \frac{\pi}{2}, \frac{3\pi}{2}, \frac{2\pi}{3}, \frac{4\pi}{3}$

7. $(\tan x - 1)(\sec x - 1) = 0 \quad \frac{\pi}{4}, \frac{5\pi}{4}, 0$

8. $\sin^3 x = \sin x \quad 0, \pi, \frac{\pi}{2}, \frac{3\pi}{2}$

9. $4(1 - \cos^2 x) = 1 + 4\cos x \quad \frac{\pi}{3}, \frac{5\pi}{3}$

10. $2\sin^2 x + 3\sin x + 1 = 0 \quad \frac{7\pi}{6}, \frac{11\pi}{6}, \frac{3\pi}{2}$

11. $2\cos^2 x - \sin x = 1 \quad \frac{\pi}{6}, \frac{5\pi}{6}, \frac{3\pi}{2}$

12. $2\sin^2 x = 3(1 - \cos x) \quad \frac{\pi}{3}, \frac{5\pi}{3}, 0$

13. $\csc^2 x = \cot x + 1 \quad \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{4}, \frac{5\pi}{4}$

14. $\sin(3x) = -1 \quad \frac{\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6}$

15. $\tan\left(\frac{x}{2}\right) = \sqrt{3} \quad \frac{2\pi}{3}$

16. $\cos(3x) = 0 \quad \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{7\pi}{4}, \frac{3\pi}{2}, \frac{11\pi}{6}$

17. $2\sin(2x) = 1 \quad \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}$

18. $\sin x = 0.4$ (use a calculator, round to the nearest tenth) $0.4, 2.7$

19. $\sec x = -4$ (use a calculator, round to the nearest tenth) $1.8, 4.5$

20. $\cos x = -0.9$ (use a calculator, round to the nearest tenth) $2.7, 3.6$

Solving Trig Eqns

$$1. 2\cos x - 1 = 0$$

$$x = \cos^{-1}\left(\frac{1}{2}\right)$$

$$\boxed{x = \frac{\pi}{3} + 2\pi k}$$

$$\boxed{x = \frac{5\pi}{3} + 2\pi k}$$

$$2. 4\csc \theta + 6 = -2$$

$$\csc \theta = -2$$

$$\sin \theta = -\frac{1}{2}$$

$$\theta = \sin^{-1}\left(-\frac{1}{2}\right)$$

$$\boxed{\theta = \frac{7\pi}{6} + 2\pi k}$$

$$\boxed{\theta = \frac{11\pi}{6} + 2\pi k}$$

$$3. 2\sin^2 x - 1 = 0$$

$$\sin^2 x = \frac{1}{2}$$

$$\sin x = \pm \sqrt{\frac{1}{2}}$$

$$x = \sin^{-1}\left(\pm \frac{\sqrt{2}}{2}\right)$$

$$\boxed{x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}}$$

$$4. 2\cos^2 x + \cos x = 0$$

$$\cos x (2\cos x + 1) = 0$$

$$\cos x = 0 \quad 2\cos x + 1 = 0$$

$$x = \cos^{-1}(0)$$

$$x = \cos^{-1}\left(-\frac{1}{2}\right)$$

$$\boxed{x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{2\pi}{3}, \frac{4\pi}{3}}$$

$$5. \sqrt{3}\cot x + 1 = 0$$

$$\cot x = -\frac{1}{\sqrt{3}}$$

$$\tan x = -\sqrt{3}$$

$$x = \tan^{-1}\left(-\sqrt{3}\right)$$

$$\boxed{x = \frac{2\pi}{3}, \frac{5\pi}{3}}$$

$$6. 1 - \cos^2 x = 1 + \cos x + \cos^2 x$$

$$0 = 2\cos^2 x + \cos x$$

$$0 = \cos x (2\cos x + 1)$$

$$\cos x = 0 \quad 2\cos x + 1 = 0$$

$$x = \cos^{-1}(0) \quad x = \cos^{-1}\left(-\frac{1}{2}\right)$$

$$\boxed{x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{2\pi}{3}, \frac{4\pi}{3}}$$

$$7. (\tan x - 1)(\sec x - 1) = 0$$

$$\tan x - 1 = 0 \quad \sec x - 1 = 0$$

$$x = \tan^{-1}(1) \quad \cos x = 1$$

$$x = \cos^{-1}(1)$$

$$\boxed{x = \frac{\pi}{4}, \frac{5\pi}{4}, 0}$$

$$8. \sin^3 x = \sin x$$

$$\sin^3 x - \sin x = 0$$

$$\sin x (\sin^2 x - 1) = 0$$

$$\sin x (-\cos^2 x) = 0$$

$$\sin x = 0 \quad -\cos^2 x = 0$$

$$x = \sin^{-1}(0) \quad x = \cos^{-1}(0)$$

$$\boxed{x = 0, \pi, \frac{\pi}{2}, \frac{3\pi}{2}}$$

$$9. 4(1 - \cos^2 x) = 1 + 4\cos x$$

$$4 - 4\cos^2 x = 1 + 4\cos x$$

$$0 = 4\cos^2 x + 4\cos x - 3$$

$$0 = (2\cos x + 3)(2\cos x - 1)$$

$$2\cos x + 3 = 0 \quad 2\cos x - 1 = 0$$

$$x = \cos^{-1}\left(-\frac{3}{2}\right) \quad x = \cos^{-1}\left(\frac{1}{2}\right)$$

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$$\boxed{x = \frac{\pi}{3}, \frac{5\pi}{3}}$$

$$10. \sin^2 x + 3\sin x + 1 = 0$$

$$(2\sin x + 1)(\sin x + 1) = 0$$

$$2\sin x + 1 = 0 \quad \sin x + 1 = 0$$

$$x = \sin^{-1}(-\frac{1}{2}) \quad x = \sin^{-1}(-1)$$

$$\boxed{x = \frac{\pi}{6}, \frac{11\pi}{6}, \frac{3\pi}{2}}$$

$$11. 2\cos^2 x - \sin x = 1$$

$$2(1 - \sin^2 x) - \sin x = 1$$

$$2 - 2\sin^2 x - \sin x = 1$$

$$0 = 2\sin^2 x + \sin x - 1$$

$$0 = (2\sin x - 1)(\sin x + 1)$$

$$2\sin x - 1 = 0 \quad \sin x + 1 = 0$$

$$x = \sin^{-1}(\frac{1}{2}) \quad x = \sin^{-1}(-1)$$

$$\boxed{x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{3\pi}{2}}$$

$$12. 2\sin^2 x = 3(1 - \cos x)$$

$$2(1 - \cos^2 x) = 3 - 3\cos x$$

$$2 - 2\cos^2 x = 3 - 3\cos x$$

$$0 = 2\cos^2 x - 3\cos x + 1$$

$$0 = (2\cos x - 1)(\cos x - 1)$$

$$2\cos x - 1 = 0 \quad \cos x - 1 = 0$$

$$x = \cos^{-1}(\frac{1}{2}) \quad x = \cos^{-1}(1)$$

$$\boxed{x = \frac{\pi}{3}, \frac{5\pi}{3}, 0}$$

$$13. \csc^2 x = \cot x + 1$$

$$\cot^2 x + 1 = \cot x + 1$$

$$\cot^2 x - \cot x = 0$$

$$\cot x (\cot x - 1) = 0$$

$$\cot x = 0; \quad \cot x - 1 = 0$$

$$x = \cot^{-1}(0) \quad x = \cot^{-1}(1)$$

$$\boxed{x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{4}, \frac{5\pi}{4}}$$

$$14. \sin(3x) = -1$$

$$3x = \sin^{-1}(-1)$$

$$3x = \frac{3\pi}{2}, \frac{7\pi}{2}, \frac{11\pi}{2}$$

$$\boxed{x = \frac{\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6}}$$

$$15. \tan\left(\frac{x}{2}\right) = \sqrt{3}$$

$$\frac{x}{2} = \tan^{-1}(\sqrt{3})$$

$$\frac{x}{2} = \frac{\pi}{3}$$

$$\boxed{x = \frac{2\pi}{3}}$$

$$16. \cos(3x) = 0$$

$$3x = \cos^{-1}(0)$$

$$3x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}, \frac{9\pi}{2}, \frac{11\pi}{2}$$

$$\boxed{x = \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{3\pi}{2}, \frac{11\pi}{6}}$$

$$17. 2\sin(2x) = 1$$

$$2x = \sin^{-1}\left(\frac{1}{2}\right)$$

$$2x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}, \frac{17\pi}{6}$$

$$\boxed{x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}}$$

$$18. \sin x = 0.4$$

$$x = \sin^{-1}(0.4) \quad 1^{\text{st}}, 2^{\text{nd}} \text{ quad}$$

$$x = .412 \quad \boxed{x = .4, 2.7}$$

$$x = \pi - .412$$

$$19. \sec x = -4$$

$$\cos x = -\frac{1}{4}$$

$$x = \cos^{-1}\left(-\frac{1}{4}\right) \quad 2^{\text{nd}}, 3^{\text{rd}} \text{ quad}$$

$$x = 1.823$$

ref \angle is $\pi - 1.823$
1.318

$$x = \pi + 1.318$$

$$\boxed{x = 4.5 \neq 1.8}$$

$$20. \cos x = -0.9$$

$$x = \cos^{-1}(-0.9) \quad 2^{\text{nd}}, 3^{\text{rd}} \text{ quad}$$

$$x = 2.691$$

ref \angle is $\pi - 2.691 = .451$
 $x = \pi + .451$

$$\boxed{x = 2.7 \text{ and } 3.6}$$